

# PSEUDO-TRISECTIONS

of

## 4-MANIFOLDS

## WITH BOUNDARY

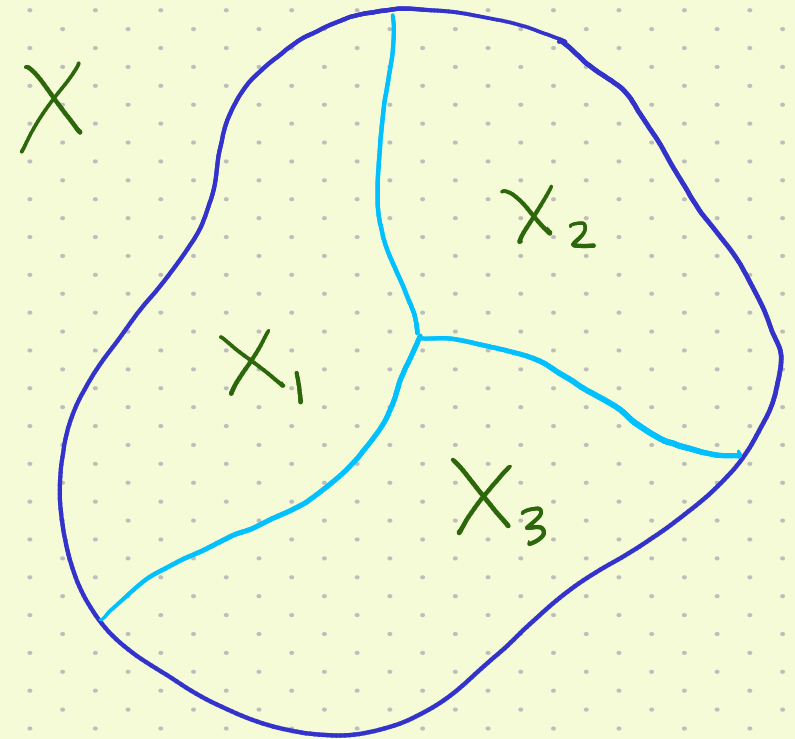
SHINTARO FUSHIDA-HARDY

STANFORD UNIVERSITY

# TRISECTIONS

GAY, KIRBY (2012)

4-MANIFOLD  $\rightsquigarrow$  THREE  
1-HANDLEBODIES



# TRISECTIONS

GAY, KIRBY (2012)

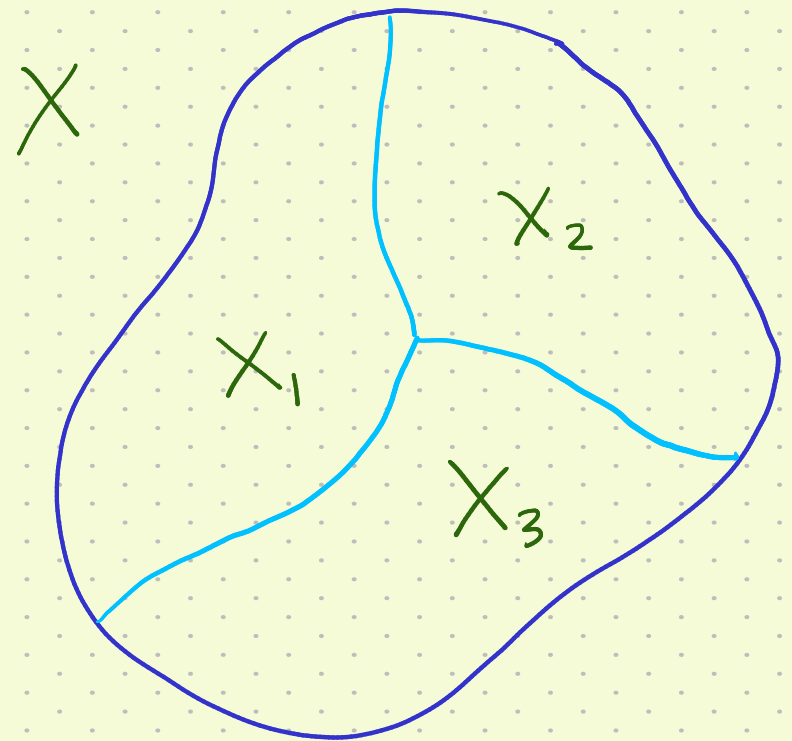
4-MANIFOLD  $\rightsquigarrow$  THREE  
1-HANDLEBODIES

RUBINSTEIN, TILLMANN (2018)

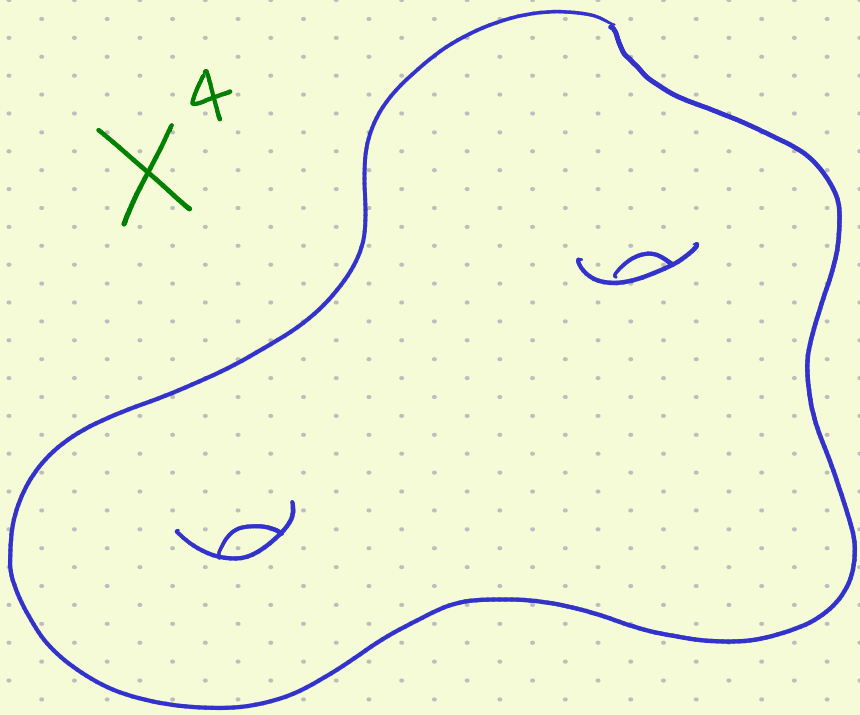
(PL)  $n$ -MANIFOLD  $\rightsquigarrow \lfloor \frac{n}{2} \rfloor + 1$   
1-HANDLEBODIES

KOENIG (2018)

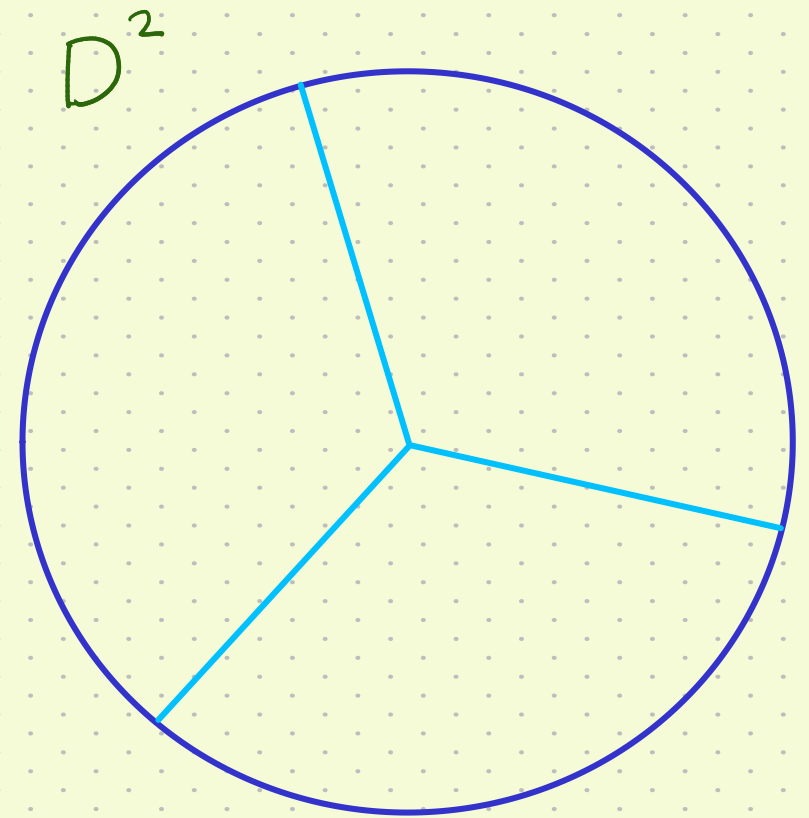
3-MANIFOLD TRISECTIONS



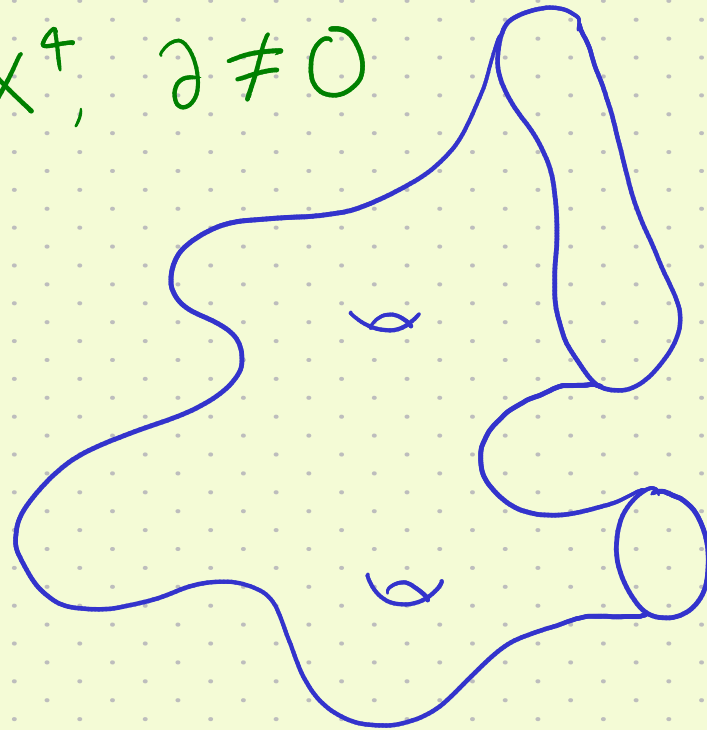
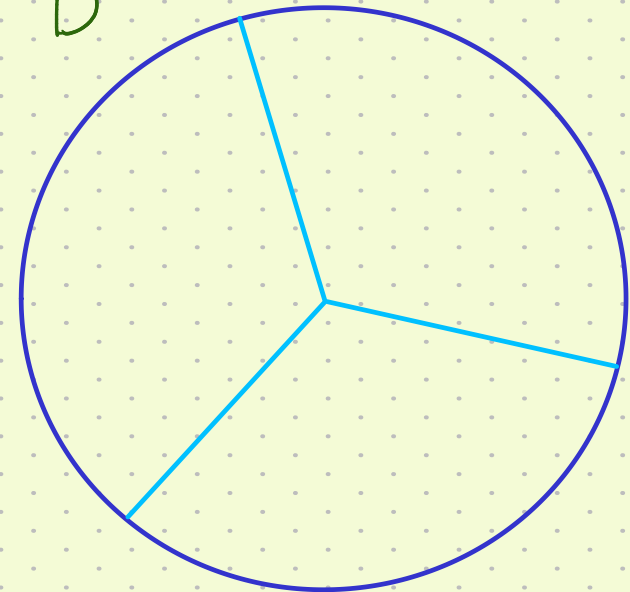
WHERE DO THEY COME FROM?



PULLBACK  
←-----  
MORSE →

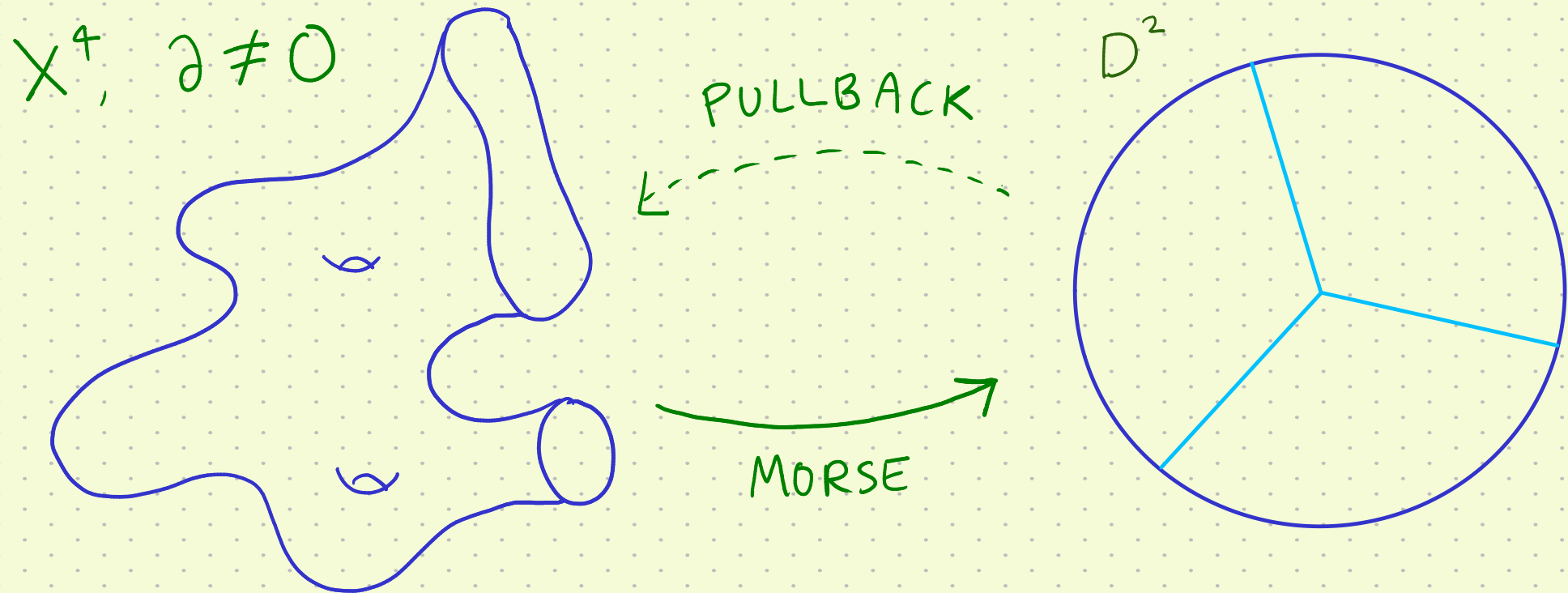


## RELATIVE TRISECTIONS

GAY, KIRBY,  
CASTRO $X^4, \partial \neq \emptyset$ PULLBACK  
MORSE  
 $D^2$ 

# RELATIVE TRISECTIONS

GAY, KIRBY,  
CASTRO

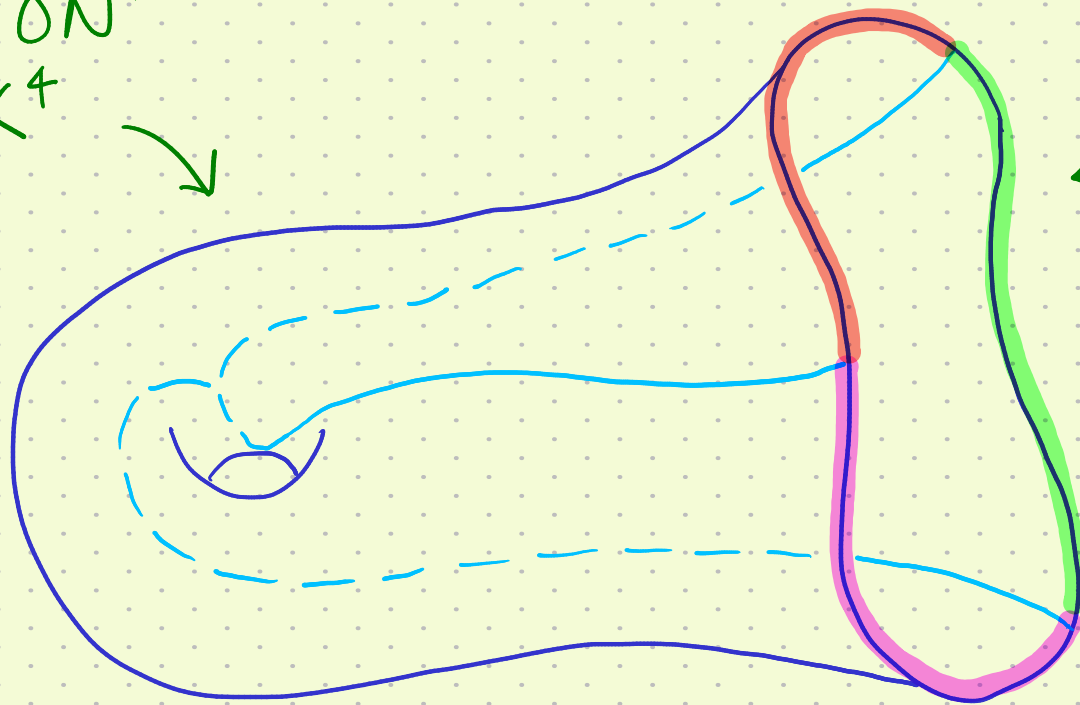


- WELL BEHAVED (GLUING ETC)
- $\partial X$  INHERITS AN OPEN BOOK
- A BIT COMPLICATED (FOR ME)

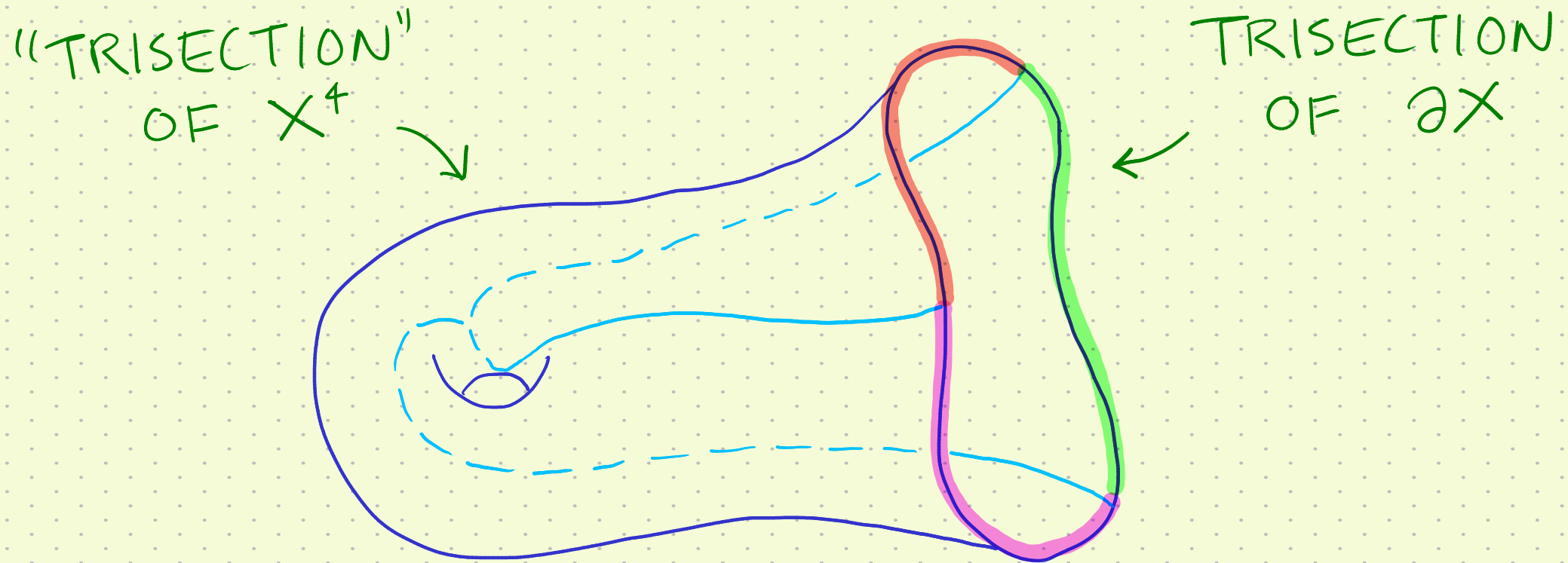
WHAT IF IT WAS TRISECTIONS  
ALL THE WAY DOWN?

# "TRISECTION" OF $X^4$

# TRISECTION OF $\angle X$



WHAT IF IT WAS TRISECTIONS  
ALL THE WAY DOWN?

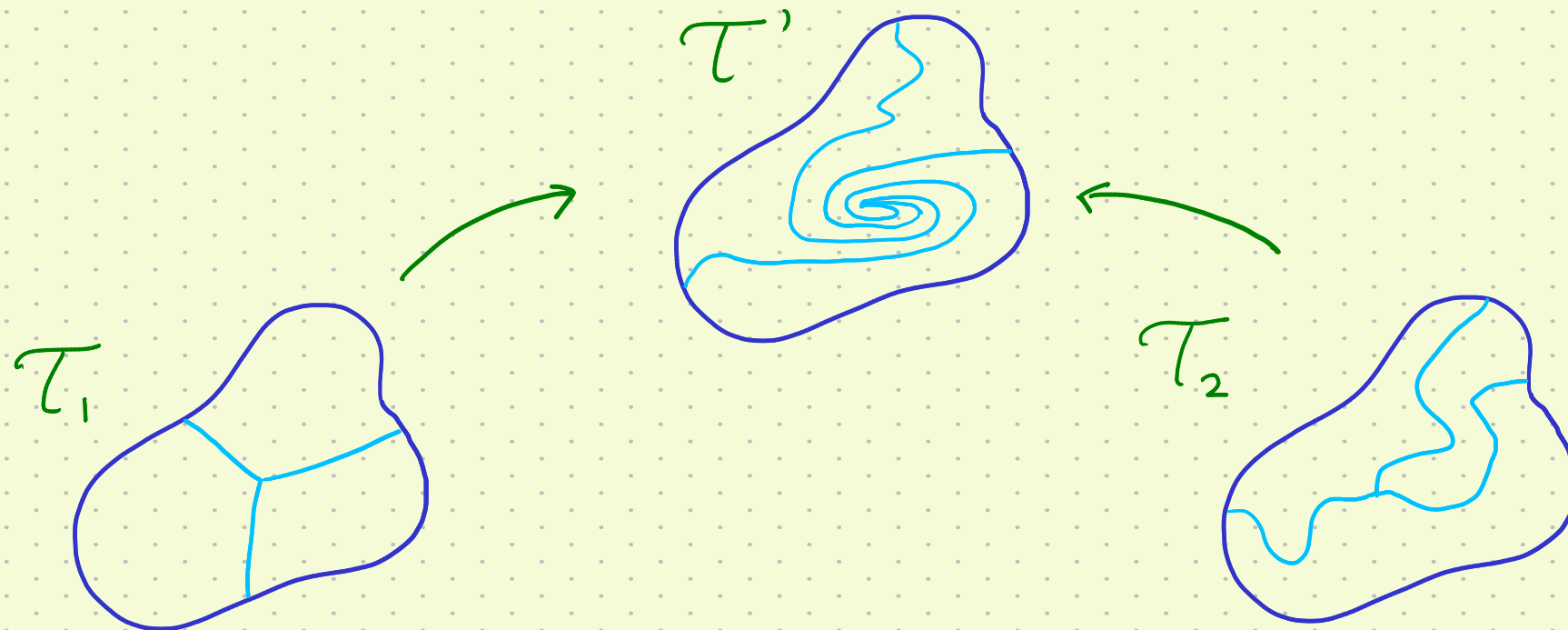


PSEUDO-TRISECTION (F.-H., 24)

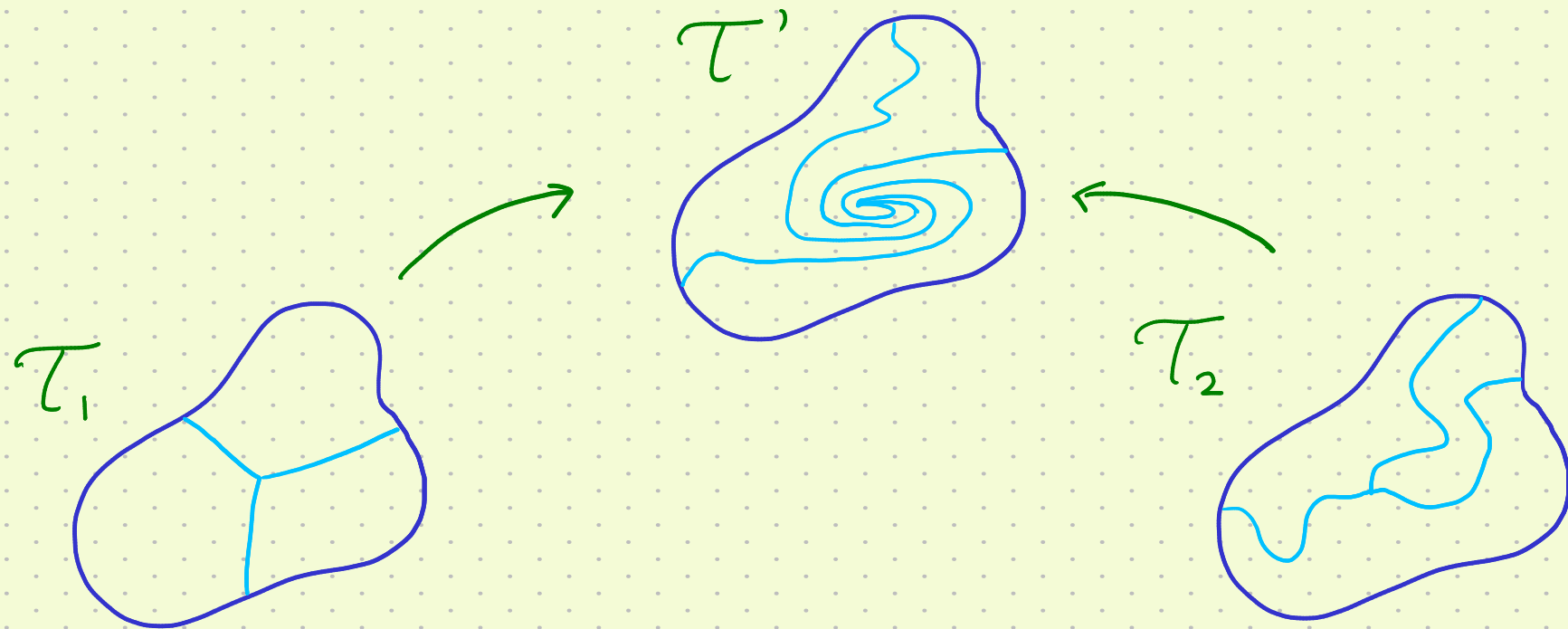
- GENERALISATION OF RELATIVE TRISECTIONS
- MANY PROPERTIES PERSIST



## STABLE EQUIVALENCE



# STABLE EQUIVALENCE

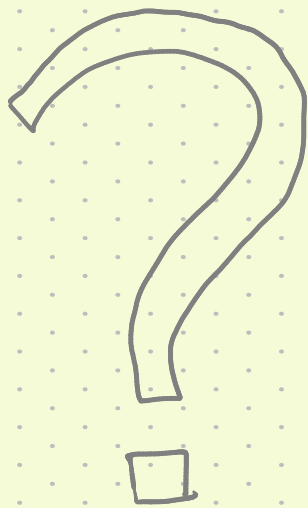
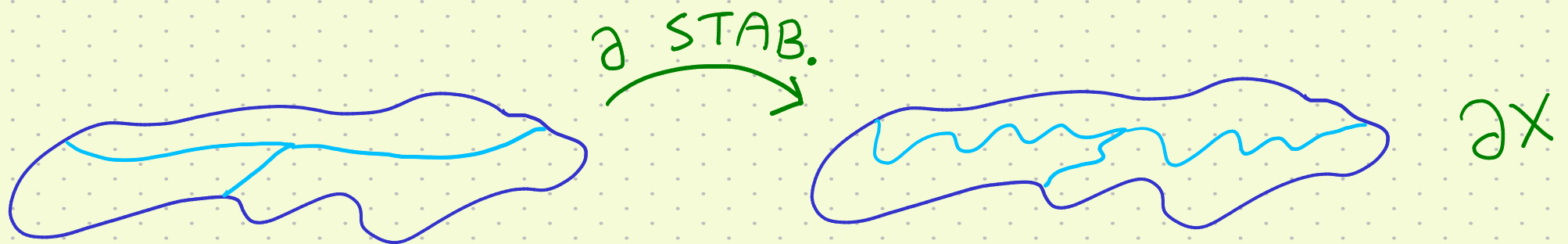


X CLOSED (TRISECTIONS) - - - - - STABILISATION

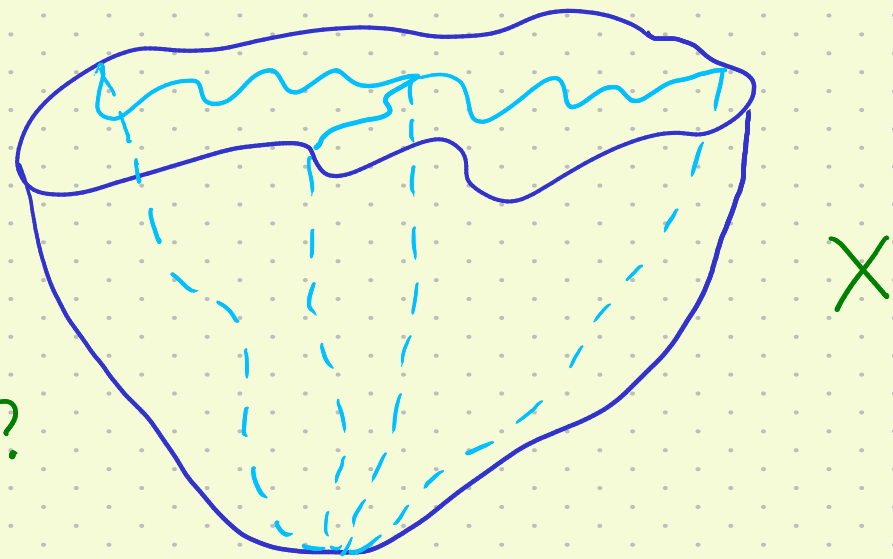
RELATIVE TRISECTIONS - - - - -  $\left\{ \begin{array}{l} \text{INTERNAL STABILISATION} \\ \text{RELATIVE STABILISATION} \\ \text{RELATIVE DOUBLE TWIST} \end{array} \right.$

PSEUDO-TRISECTIONS - - - - -  $\left\{ \begin{array}{l} \text{INTERNAL STABILISATION} \\ \text{BOUNDARY STABILISATION} \\ \text{HEEGAARD STABILISATION} \end{array} \right.$

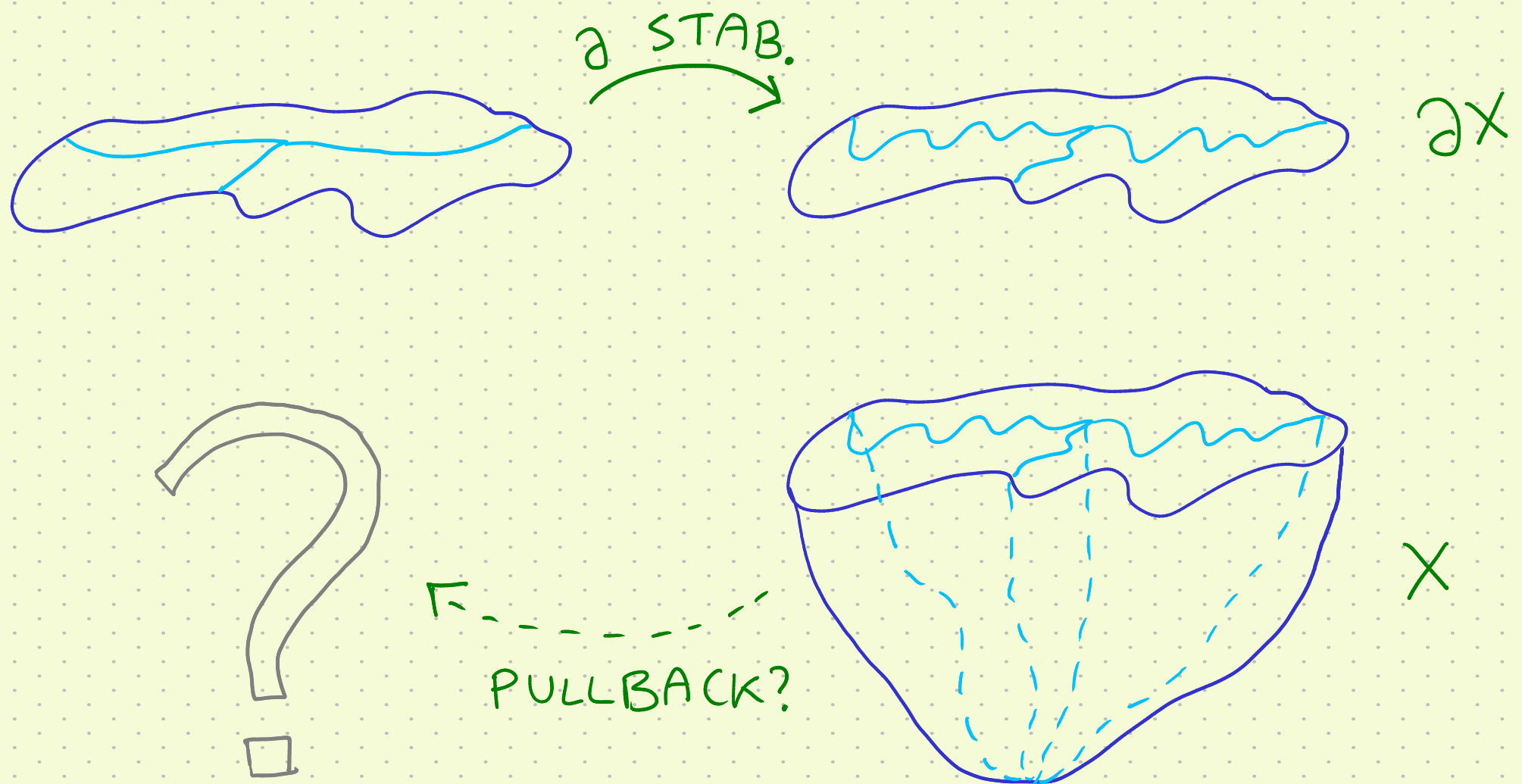
## DESTABILISATION?



PULLBACK?



# DESTABILISATION?



YES! (FOR PSEUDO-TRISECTIONS)

THANK YOU!